

Electronics
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Module No. # 07
Differential & Operational Amplifiers
Lecture No. #04
Operational Amplifiers in Open Loop

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Lecture: 37 Module VII 10/05/11

op amps in open loop:
(that is op amp without feedback network).

$A = \text{open loop gain of the op amp.}$
(741)
 $A = 10^5$

$v_o = A \times v_i$
 $= 10^5 \times 1 \times 10^{-3}$
 $v_o = 100V$

v_o - output will saturate at $+V_{sat} = V_{cc}$

The diagram shows an operational amplifier with the non-inverting input (+) connected to an input signal v_i and the inverting input (-) connected to ground. The output is connected to a load resistor R_L . The supply rails are labeled $+V_{cc}$ and $-V_{EE}$. The open-loop gain is denoted as A .

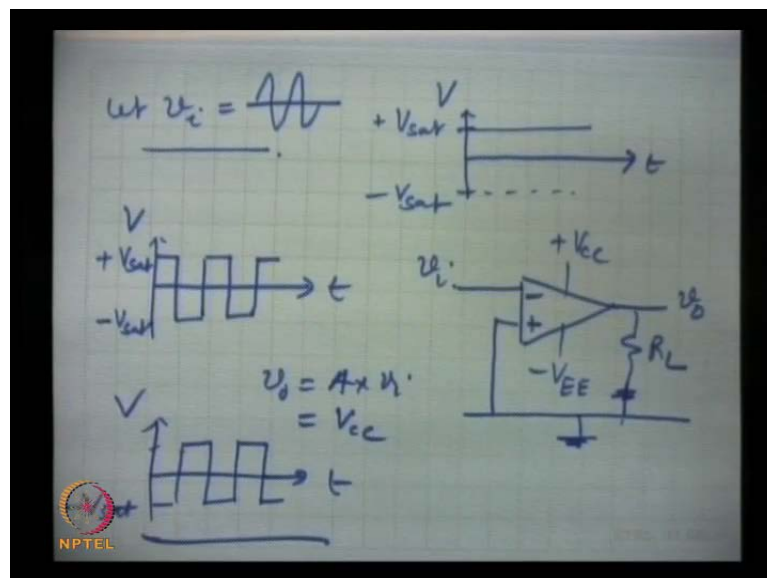
I have been discussed the basics of operational amplifiers, we continue to study them for example, how they can be used, and what are their circuit applications. First we take op amps in open loop, by open loop we mean that there is no feedback involved in it; that means, that is op amp without feedback **op amp without feedback** network. How will it behave, just let us consider a op amp with the two inputs as we have said. So, let us take that in open loop this is non inverting input to which we apply a input signal and let this inverting input b grounded.

Now, this A is the open loop voltage gain and v out we take from here R_L , and this is v out. Now this A is the open loop gain, always remember open loop gain **gain** of the op amp and the 741 op amp, 741 which is a general purpose op amp and that we are taking

as the model just a sample we used. So, this 741 has A around 10 to the power 5 its 100000 is the voltage gain. Now let us see what will happen if we apply A for example, a positive signal v_i is plus 1 mill volt let us say this is d c.

Now, mathematically what will be the output, the output is gain into input that is, this v out will be A into v_i gain is 10 to the power 5 **ten to the power five** and this is 1 milli volt. So, 1 is to 10 to power minus 3 volt. So, the simple mathematic says that v out will be 100 volts. Now very fundamental thing that in a circuit this v out the output voltage cannot exceed the maximum d c voltage is available or applied to the circuit. Therefore, this instead of 100 it will saturate at V_{sat} output v out that is output we will saturate at plus V_{sat} .

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And V_{sat} normally will be slightly low, but of the order of V_{cc} , the V_{cc} is 15 volts then plus V_{sat} will be roughly 14 or 14.5 volts. So, it will saturate. So, what we will get with the **inverter** non inverting signal the output will be like this, this is a time, this is a voltage and this is V_{sat} this is minus V_{sat} . So, if the voltage is positive it will just saturate here and if it is negative voltage here, if this voltage is negative then without change of polarity it will appear n output and it will saturate A.

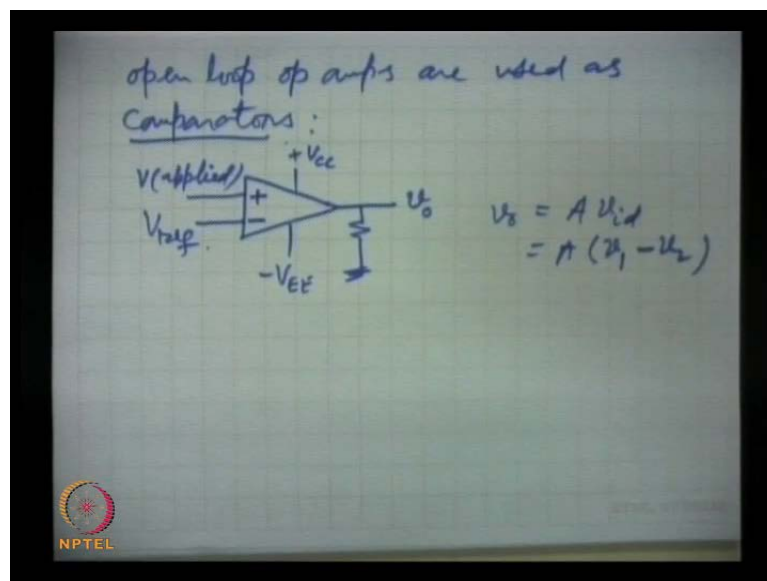
Now, if we apply a sinusoidal signal let v_i b sinusoidal like this, this is the input signal and the if this is say of the order of a milli-volt then same thing will happen here. It will just saturate at plus V_{sat} and here it will saturate at minus V_{sat} . So, if this is the input

the output will be this. This is the output voltage time plus V_{sat} and here this is minus V_{sat} , this is highly distorted this is not the replica of the input. Therefore, does in open and loop A op amp amplifier is a rarely used almost never used as an amplifier because output will be a kind of square wave for a sinusoidal signal.

So, this is highly distorted when we compare the two. The same thing will happen when we apply the input instead of a the non inverting input if we apply at the inverting input, all voltages are always with respect to ground. When we say v_i this is like this actually here this is the ground level and this is grounded and here we apply a voltage this is the inverting input and v_i and this is the output which is a gain with respect to ground this is v_o this is the load. So, this is not shown, but in a statement we cover it that all voltages output and input voltages are with respect to ground.

So, here when we apply it the sign will be inverted if it is d c if we apply a positive voltage it will saturate at a minus V_{sat} and if it is negative voltage, it will saturate at plus V_{sat} and we apply a sinusoidal signal and if this exceeds the limit A into v_i more than V_{cc} , then it will produce a signal at output A square wave with inversion. That means, **the** it will be like this, this is time, this is minus V_{sat} plus V_{sat} and this is voltage. So, this is n if we apply use it as a differential amplifier.

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Then the difference of the two will be will appear will again normally, it will saturate. Unless the difference is in say micro volts then of course, amplified signal will appear.

Now, **what** how we summarize this? That normally as an amplifier in open loop op amps are not used; sometimes they can be used as comparators open loop op amps are used as comparators; comparators is a circuit which compares two voltages. So, here for example, we give here a, one is the reference this is a reference voltage.

And this is the applied voltage, we applied to be compared applied means the one which you want to compare. Now the output when we take, then as soon as this will exceed this, the output will saturate accordingly and a signal will be available. So, this way the three configurations in open loop the inverting amplifier, non inverting amplifier and as a difference amplifier this is a not used as an amplifier, but one of the applications for open loop is as comparators where v_0 will be $A v_i$ and $A v_1$ minus v_2 , where one of these can be a reference voltage.

So, this can be used **as an** as an comparator,; but the use of op amps as an amplifier is very wide **very wide** as I said there are a large number of applications of op amps. But most of these applications are with the using proper feedback and the amplifier realization that is construction of a amplifier is simplest with a op amp. We can choose how much gain we will see we are coming to that **that**, we can choose how much gain for the amplifier is required and what is the input impedance we want. Then we have choose just two, three resistances of a rap appropriate value they are to be attached with the op amp.

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OP-AMPS AS AMPLIFIERS
 Non-inverting amplifier with feedback
 (negative feedback).

$A = \text{open loop gain}$
 $A = 10^5$

$$v_o = A(v_1 - v_2)$$

In the fig, $v_1 = v_i$
 $v_2 = \text{Voltage feedback to inverting input}$

The diagram shows an operational amplifier with the non-inverting input (+) connected to an input terminal labeled v_i . The inverting input (-) is connected to a feedback network consisting of two resistors, R_1 and R_F . Resistor R_1 is connected between the inverting input and ground, and resistor R_F is connected between the output and the inverting input. The output terminal is labeled v_o . The power supply rails are labeled $+V_{CC}$ and $-V_{EE}$. A hand is visible at the bottom right, holding a pen and pointing towards the diagram.

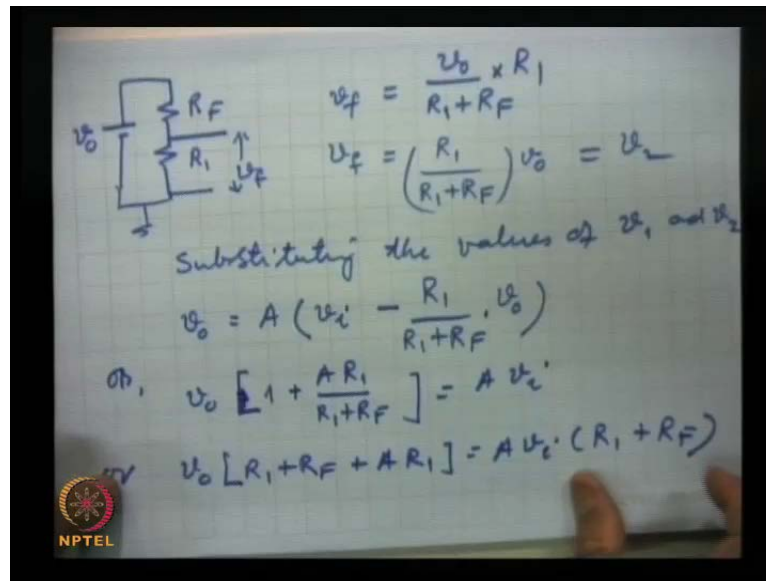
And the design will be extremely simple you need not to bother about biasing network this and that, that is all everything has been taken care of by the manufacturer and designing the op amp. So, we take the applications of **amplifier** of op amp as amplifier first. So, op amp as amplifier op amps as amplifier there are three amplifiers and all three we will take one by one. First, we take non inverting amplifier **non inverting amplifier** with feedback and this feedback is negative feedback, in amplifiers we always use negative feedback.

This point was stated and made clear when we were discussing a feedback in amplifiers negative feedback. First, let us see what will be the simple circuit and then we analyze this amplifier. This is v_{out} and this is the input and the feedback is this R_F this resistance is R_F and this is R_1 look at the simplicity of the circuit and of course, these sources are there plus V_{cc} and minus V_{cc} . Even if we do not show these two d c supplies it is implied no electron circuit will work **with a** without a d c supply.

Because, d c voltages are needed for biasing the transistors which is too important for biasing is too important for the operation of any transistor. So, this is the circuit and this we analyze and since the input signal has been connected with the non inverting input which is indicated by plus sign. So, this is a non inverting amplifier with a proper feedback now we analyze it and remember A many times written here, A is the open loop gain **open loop gain**, gain without feedback. This is the feedback amplifier how much will be the gain that we will estimate and evaluate for this, but this is provided by the manufacturer open loop gain.

And for most of the amplifiers particularly 741 this is A is 100000, 10^5 . Now the v_{out} this v_{out} identify this is v_1 and this is v_2 , now v_{out} this v_{out} simply this is gain and the difference of two voltages v_1 minus v_2 , whatever is the voltage here that is v_1 and whatever is the voltage here that is v_2 . So, the difference of this will be **will be** multiplied with the gain will be the output, if we take in this figure, in the figure **in the figure** v_1 this v_1 is equal to v_i this two are identical. So, v_1 is v_i and v_2 **v_2** will be the voltage here feedback voltage.

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This is we write v_f , v_f is voltage feedback to inverting **inverting** input and this is simple, this we have talked several times, but anyway I do this. Voltage here is v_0 and these are two resistance and what will be the voltage drop here, this is voltage divider circuit, which I can drawn like this actually this is $R_F R_1$ and whatever is the voltage drop here, this is v_f the feedback voltage and this is v_0 see here v_0 and this resistance these two resistance is they are dividing this voltage.

So, this is the network. How much will be v_f the current will be $v_0 R_1$ plus R_F , this is the current through these resistance is which are in series and the voltage drop across R_1 will be the current, **this is a current actually** this is the current and multiplied with R_1 becomes the voltage. So, v_f is R_1 by R_1 plus R_F v_0 simple voltage divider circuit and this we have talked several times. This is the current which will be flowing and what will be the voltage drop across this multiplied with R_1 that is this voltage v_f . So, we substitute the value of v_1 substituting the values of v_1 .

And v_2 this v_f this is a equal to v_2 the voltage here with respect to ground is the same as voltage v_f . So, this is v_2 and v_1 we already have this. So, when we substitute v_1 and v_2 we get v_0 is a v_1 , v_1 was v_i minus v_2 , v_2 is this. So, $R_1 R_1$ plus R_F into v_0 ; so this is simply v_0 equal to A into v_1 minus v_2 , we have **substitute the** substituted the values of v_1 and v_2 and this we can write or we take this term here or v_0 is v_0 into 1 plus $A R_1$, R_1 plus R_F this is a v_i let us $0 r$ across multiplication.

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The image shows a handwritten derivation on a whiteboard. At the top, the exact closed-loop gain is given as $A_{FB} = \frac{v_o}{v_i} = \frac{A(R_1 + R_F)}{R_1 + R_F + AR_1}$ (Exact). A note in parentheses says "(Gain with feedback in closed loop gain)". Below this, it says "Normally ~~AR1 >> R1 + RF~~ $AR_1 \gg R_1 + R_F$ ". The next line shows the simplified gain: $A_{FB} = \frac{A(R_1 + R_F)}{AR_1} = 1 + \frac{R_F}{R_1}$. The final line shows the simplified gain again: $A_{FB} = 1 + \frac{R_F}{R_1}$. An NPTEL logo is visible in the bottom left corner of the whiteboard image.

We will give $A \theta R_1$ plus R_F plus $A R_1$ this is equal to $A v_i R_1$ plus R_F and now from here, we can get the close loop gain from this the expression we will get A with feedback. So, normally we write with F or FB with feedback gain **gain** with feedback, that is A_{FB} is closed loop gain **closed loop closed loop gain** this is equal to v_o by v_i here input signal was v_i output v_o . So, ratio of output voltage to input voltage is the gain this is the op amp in open loop and this is the feedback network.

So, this whole amplifier is A and amps which feedback this is amps which feedback for that, this is the gain and which from this equation v_o by v_i , this becomes equal to $A R_1$ plus $R_F R_1$ plus R_F plus $A R_1$, this is the exact expression we write here exact. This is the exact expression for the voltage gain, but when we see the practical situation it gets drastically simplified and the situation is that normally and normally means most of the time $A R_1$ is very, very large as compare to R_1 plus R_F , R_1 into A , A is 10 to the power 5; so, 100000 times R_1 , while this resistance is made differ early by effect of 2 or 3 or 5. So, this is this condition will be mostly available and applicable. So, this we can or this can be neglected and then gain which feedback becomes equal to $A R_1$ plus R_F by $A R_1$ or simple $1 + \frac{R_F}{R_1}$. This is the gain of the non inverting amplifier with feedback is $1 + \frac{R_F}{R_1}$, how simple you choose the gain how much you want 10, 20, 30, 50, 100 accordingly choose these two resistances if for example.

Now, because this is an op amp is a small signal device. So, resistance is normally will be ohms because ratios suppose we want a gain of 20. Let A_{FB} desired is 20 and for that from this expression, we want R_F by R_1 ratio be to 19. Now 19 you can have for example, R_F you can choose a say 190 into 2; so many ohms and R_1 , because this is to be 20 this ratio as to be 20. So, this becomes 380, 380 divided by 20.

So, 20 ohms and 380 ohms if we take ratio will be 19, but these resistance is will draw it large current and the currents will exceed the maximum current which is recommended for the op amps and op amps will be burn. So, instead of in ohms these are taken in clones. So, we can choose β this in clones and we can have this ratio 19 then gain will be 20. For example, let R_F be 19 clones and R_1 v 1 ohm then gain A_{FB} will be 1 plus 19 k by 1 k. So, this is 20 gain will be 20 how simple it is to construct a non inverting amplifier with a desire gain.

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$$v_2 = v_f = \left(\frac{R_1}{R_1 + R_F} \right) v_0$$

$$\beta = \frac{v_f}{v_0} = \frac{R_1}{R_1 + R_F}$$

using $\frac{R_1}{R_1 + R_F} = \beta$ in

$$A_{FB} = \frac{A(R_1 + R_F)}{R_1 + R_F + AR_1} = \frac{A}{1 + A \frac{R_1}{(R_1 + R_F)}}$$

$$A_{FB} = \frac{A}{1 + AB} \quad AB \gg 1 \quad A_{FB} = \frac{1}{\beta}$$

$1 + AB$

Now, let us go further to show that non inverting amplifier with amps is a very close to an ideal voltage amplifier. It is an ideal voltage amplifier and this we can show by using the concepts of feedback. Now from this equation v_2 equal to v_f which was equal to voltage divider R_1 plus R_f into v_0 this is v_f , you remember that in the feedback networks $1 + AB$, where AB is the close loop gain and beta A factor. So, beta is v_f by v_0 the fraction which is written 2, this is the input of this is the feedback network the input.

Here was v_0 this v_0 is the input to the feedback network and output we are taking here. So, the gain of **of of** feedback network is output divided by input v_f by v_0 which from here we write as $\frac{R_1}{R_1 + R_F}$. This is **the the** gain of the feedback network and then using this expression using $\frac{R_1}{R_1 + R_F} = B$, in the $A F$ the exact equation, which was $A \frac{R_1}{R_1 + R_F} + R_F = A R_1$. If we use this then this can be written as $A F B = A + A B$ just substitute like this.

And this becomes this we divide by R_F actually. So, this is A by $1 + A B$ $\frac{R_1}{R_1 + R_F}$ which this is B . So, this is this expression which was the expression for a voltage amplifier with the negative feedback and this term $A B$ will be very large in comparison to 1. So, 1 can be drop. So, the gain $A F B$ is $\frac{1}{B}$ that is highly stable. The gain of the feedback amplifier op amps does not depend on variations in A which may vary because of aging or temperature or noise in the surroundings whatever may be the reasons, but the gain of the feedback amplifier the of the no inverting operational amplifier with feedback is stable.

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Handwritten notes on a whiteboard showing the derivation of the closed-loop gain and input/output impedances for a feedback amplifier.

$$A_{FB} = \frac{A}{(1 + AB)}$$

Input impedance increases:

$$R_{iF} = R_i (1 + AB)$$

$R_i =$ input w/o feedback.

output impedance is reduced.

$$R_{oF} = \frac{R_o}{(1 + AB)}$$

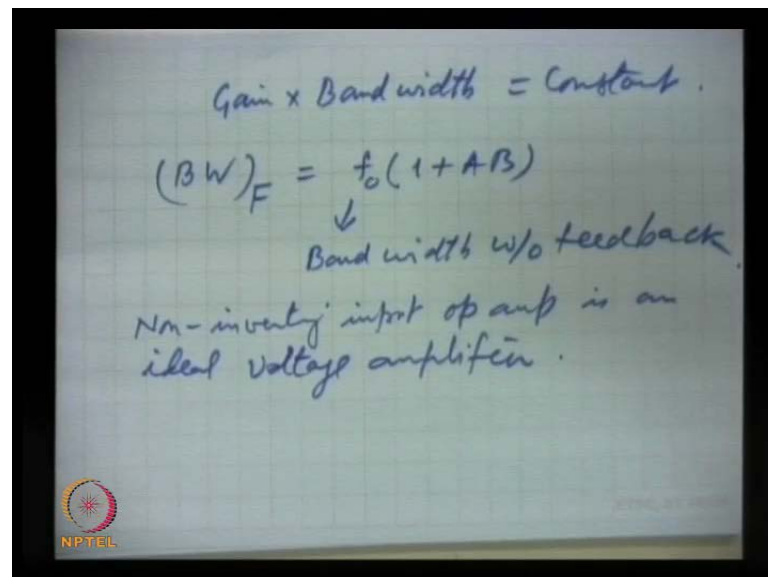
NPTEL logo is visible in the bottom left corner of the whiteboard image.

And it simple depends on the B , the B network is normally few resistances. So, with this expression every quantity will vary with the you remember we said this which feedback that because, the gain is $A + A B$ and all qualities will vary either increase or decrease by a factor $1 + A B$. If we increase we have multiply by this factor and if they fall will have to divide it. So, **this is** this amps here the sacrifices what we are doing

that gain falls from A to this, the gain of the non inverting amp with feedback is much reduced it is reduced by this factor 1 plus A B and this factor may be 100.

So, then the gain will fall by hundred 10 to the power 5 by 100 even 1000. So, if it is 1000 this factor is 1000 it will be just 100 may be less. So, now what are the quantities we recollect from our discussion in the feedback chapter which we finished that input impedance, input impedance with feedback that is $R_i F$ with feedback this is R_i and it increases by this factors. If this is R_i is the input without feedback then this is the input impedance it will increase by this factor.

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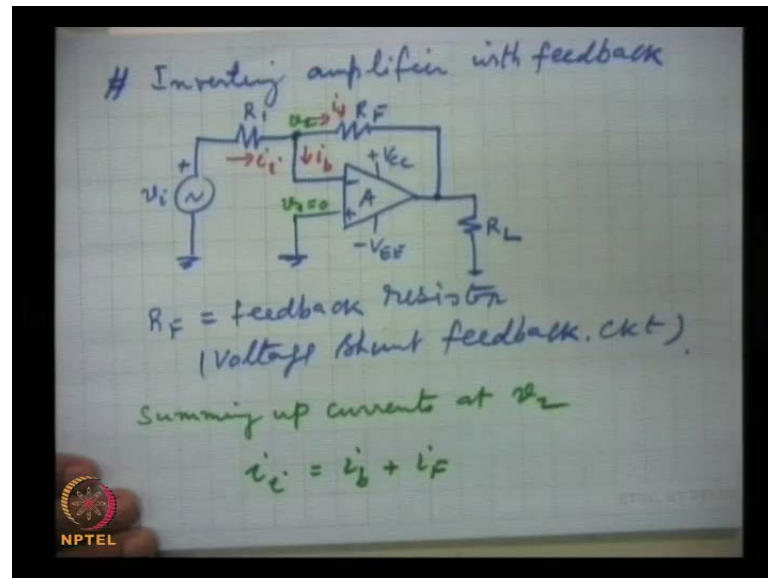


And this factor is for example, often 1000 10 and more see 1000 times the input impedance will increase and the output impedance, in this case we will reduced the output impedance **is reduced** is reduced and with feedback $R_o F$. If without feedback it is R_o then this 1 plus A B, it will be reduced and a ideal or rather a good voltage amplifier is suppose to have high input impedance and low output impedance and band width will increase because you will recall that gain width product is constant gain voltage gain into band width product is a constant for a device in this case gain falls by a factor 1 plus A B.

Hence the band width increase by the same factor 1 plus A B. So, **with feedback band width** band width with feedback this is, if this is the band width without feedback, then it will be this is band width without feedback. So, we are seeing all through that non

inverting op amp is a non inverting amp is an ideal voltage amplifier, non inverting input op amp which is called actually non inverting op amp is an ideal voltage amplifier. So, this is the major things about a non inverting amplifier.

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Next, we take inverting amplifier and how we know that whether the amplifier is inverting or non inverting simple. Where we are feeding the input signal as you have seen in this case the which we have studied the input signal was at as to a non inverting amplifier a non inverting input. So, it was a non inverting amplifier. Next is inverting amplifier **inverting amplifier** with feedback let us see the circuit, the circuit is this, this is the circuit for inverting amplifier just we connect two resistances R_f and R_1 .

These two resistance is externally connected then it makes a inverting amplifier and now we investigate the important properties of this circuit. Here R_f this is the feedback resistance feedback resistor and R_1 is a another resistance and we can see that this is the voltage shunt **voltage shunt** feedback circuit. Now the most important property of an amplifier is the voltage gain the other important property is input impedance and so on. So, first we take a voltage gain of this amplifier.

Let us see here this current is i_i this is i_b and this i_f , this is the input current which is divided into two parts. So obviously, summation of currents at this point which is v_2 and this is v_1 this is of course, is 0 because, it has been grounded this terminal is at potential v_2 and this is with respect to ground of course, and this is at v_1 , but v_1 is 0. So,

summing up currents at v_2 gives i_i this is equal to i_b plus i_f and i_b you remember that the input impedance of A the op amp is an extremely large it is in wave ohms.

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Handwritten mathematical derivation on a whiteboard:

$$\text{Since } i_b \approx 0$$

$$i_i = i_f$$

$$\frac{v_i - v_2}{R_1} = \frac{v_2 - v_o}{R_F} \quad \text{--- (X)}$$

$$A = \frac{v_o}{v_i - v_2} \quad \because v_1 = 0$$

$$A = -\frac{v_o}{v_2}$$

$$v_2 = -\frac{v_o}{A}$$

The NPTEL logo is visible in the bottom left corner of the whiteboard image.

So, this current is very feeble. So, since i_b is very close to zero because the input impedance of the amplifier is very high. Therefore, i_i is simply equal to i_f now what is the value of i_i and this terminal one terminal is at the voltage v_i the other terminal is at v_2 . So, what is the current flowing through this ohm law potential difference is v_i minus v_2 divided by R_1 . So, this is this current this is v_i minus v_2 by R_1 this is equal to i_f I mean i_f the two terminals of i_f one is at voltage v_2 other is at voltage v_o output voltage.

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Substituting for v_2 in eq. (x)

$$(v_i + \frac{v_o}{A}) / R_1 = (-\frac{v_o}{A} - v_o) / R_F$$

or $A_{FB} = \frac{v_o}{v_i} = -\frac{A R_F}{R_1 + R_F + A R_1}$

Since $A R_1 \gg R_1 + R_F$

$$A_{FB} = -\frac{R_F}{R_1} \quad (\text{Practical})$$

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So, this is equal to v_2 minus v_θ by R_F and from here we can what will be the gain. The gain of the amplifier, this is equal to v_θ and two voltages v_1 by v_2 , but v_1 is 0 because it is grounded v_1 is 0. So, since v_1 is 0, A is v_0 by v_2 and of course, that is a minus sign here, from here v_2 is equal to minus v_0 by A and this we substitute let us call this equation x. In this equation we substitute this substituting for v_2 in equation x we get v_i minus v_i minus v_2 , but because v_2 is minus v_0 by A .

So, this is v_0 by A by R_1 this is equal to minus v_0 by A minus v_θ by R_F or the voltage gain with feedback. This is equal to v_0 by v_i output is v_0 input is v_i . So, this is the voltage gain of the total amplifier and this is equal to minus $A R_F$ just from here, it is simple manipulation and this is R_1 plus R_F plus $A R_1$ and since $A R_1$ is very large as compare to R_1 plus R_F . So, this we can drop and A_{FB} gain with feedback this simply is minus R_F by R_1 . How simple it is the expression for the gain of this inverting amplifier this of course, sign shows the inversion as it is we expected, because it is a inverted input, so inverting input.

So, hence this sign indicates there and just choose the desired ratio R_F / R_1 required to obtain the **the** desired gain. If gain as to be 100 choose this 100 k this as 1 k the gain will be 100 how simple it is. You cannot think an simpler amplifier in which the you choose the gains several parameters will have to adjust and several parameters you have to calculate here simply two resistances you have to take of appropriate value R_F and R_1

and this will be the **the** case. So, this is the practical this is the exact expression for the voltage gain which is rarely used.

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If we substitute $v_2 = 0$ in Eq(x),
 $v_1 - (v_2) = 0 = 0$
 $\frac{v_1}{R_1} = \frac{v_2 - v_0}{R_F}$
 $A_{FB} = -\frac{R_F}{R_1}$
Inverting input is 'virtual ground'.

Because it does not make sense while this condition is very much satisfied hence this is the practical expression. So, practical expression for the voltage gain now one very important parameter about this amplifier and that is this expression can be obtained from this equation. If we substitute v_2 equal to 0 the same expression which we have arrived here, we get if we substitute v_2 equal to 0 in equation x **in equation x**, then we will get the same here, this equation x was this v_i is v_2 v_1 is v_2 v_0 R_F .

And from here if we substitute this as 0, this is 0 then the gain A_{FB} is equal to minus R_F by R_1 same expression means sure, we have a obtained ever that is here we got the same thing if this consideration, but the same expression we get with v_2 equal to 0. What is v_2 equal to 0 this is v_2 , v_2 equal to 0 means that v_2 is at the ground potential **ground potential** it is called virtual ground. The inverting input very important inverting input is virtual ground **virtual ground**. Why ground because at ground potential and why virtual because, actual ground can take almost any amount of current hundred thousand amperes whatever, but here you know only milli amperes can be observed in the device.

So, it is virtual ground this concept remember that inverting input is a virtual ground it is at ground potential this is a great hell in simplifying the analysis of more involved circuit like summing integrator differentiated, which we **we** are going to be studied. So,

remember two things the gain of the inverting amplifier is just the ratio R_F and R_1 , choose these appropriate values for the desired gain, and the inverting input is a virtual ground and we will continue our discussion. This is very important point remember that inverting input is a virtual ground it is at ground potential.